

1) Evaluate the iterated integral.

a) $\int_0^1 \int_0^{x^2} (x + 2y) \, dy \, dx$

b) $\int_0^1 \int_y^{e^y} \sqrt{x} \, dy \, dx$

c) $\int_0^{\pi/2} \int_0^{\cos y} e^{\sin y} \, dx \, dy$

a) $\frac{9}{20}$

b) $\frac{4}{9}e^{3/2} - \frac{32}{45}$

c) $e - 1$

2) Evaluate the double integral.

a) $\iint_D x \cos y \, dA$, D is bounded by $y = 0$, $y = x^2$, $x = 1$

b) $\iint_D y^3 \, dA$, D is the triangular region with vertices $(0, 2)$, $(1, 1)$, $(3, 2)$

c) $\iint_D (2x - y) \, dA$, D is bounded by the circle with center at the origin and radius 2.

a) $\frac{1}{2}(1 - \cos 1)$

b) $\frac{147}{20}$

c) 0

3) Find the volume of the given solid:

- a) Enclosed by the paraboloid $z = x^2 + 3y^2$ and the planes $x = 0$, $y = 1$, $y = x$, $z = 0$.
- b) Bounded by the cylinder $x^2 + y^2 = 1$ and the planes $y = z$, $x = 0$, $z = 0$ in the first octant.

a) $\frac{5}{6}$

b) $\frac{1}{3}$

4) Find the volume of the solid by subtracting two volumes. The solid enclosed by the parabolic cylinders $y = 1 - x^2$, $y = x^2 - 1$ and the planes $x + y + z = 2$, $2x + 2y - z + 10 = 0$.

$$\frac{64}{3}$$

5) Evaluate the integral by reversing the order of integration:

a) $\int_0^3 \int_{y^2}^9 y \cos(x^2) dx dy$

b) $\int_0^1 \int_{\arcsin y}^{\pi/2} \cos x \sqrt{1 + \cos^2 x} dx dy$

a) $\frac{1}{4} \sin 81$

b) $\frac{1}{3} (2\sqrt{2} - 1)$

6) Find the average value of $f(x, y) = e^{x+y}$ over the region R represented by the triangle with vertices $(0, 0)$, $(0, 1)$, $(1, 1)$.

$$(e-1)^2$$